# **Study Guide and Intervention**

# **Graphing Exponential Functions**

**Exponential Growth** An exponential growth function has the form  $y = b^x$ , where b > 1. The graphs of exponential equations can be transformed by changing the value of the constants a, h, and k in the exponential equation:  $f(x) = ab^{x-h} + k$ .

Parent Function of **Exponential Growth** Functions,

 $f(x) = b^x, b > 1$ 

- 1. The function is continuous, one-to-one, and increasing.
- 2. The domain is the set of all real numbers.
- **3.** The *x*-axis is the asymptote of the graph.
- **4.** The range is the set of all non-zero real numbers.
- **5.** The graph contains the point (0, 1).

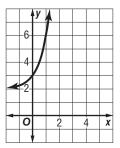
#### Example

### Graph $y = 4^x + 2$ . State the domain and range.

Make a table of values. Connect the points to form a smooth curve.

Х	-1	0	1	2	3
у	2.25	3	6	18	66

The domain of the function is all real numbers, while the range is the set of all positive real numbers greater than 2.

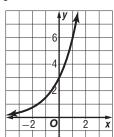


Lesson 7-1

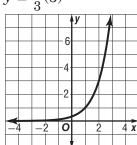
## **Exercises**

Graph each function. State the domain and range.

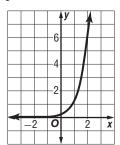
1. 
$$y = 3(2)^x$$



**2.** 
$$y = \frac{1}{3}(3)^x$$



$$3. y = 0.25(5)^x$$



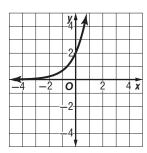
 $D = \{all real numbers\};$ 

 $R = \{y | y > 0\}$ 

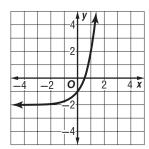
$$R = \{y | y > 0\}$$

$$R = \{y | y > 0\}$$

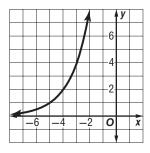
**4.** 
$$y = 2(3)^x$$



**5.** 
$$y = 4^x - 2$$



**6.** 
$$y = 2^{x+5}$$



 $D = \{all real numbers\};$ 

 $R = \{v | v > 0\}$ 

 $R = \{y | y > -2\}$ 



#### **Study Guide and Intervention** 7-1

(continued)

# **Graphing Exponential Functions**

**Exponential Decay** The following table summarizes the characteristics of **exponential** decay functions.

**Parent Function of Exponential Decay** Functions,  $f(x) = b^x, 0 < b < 1$ 

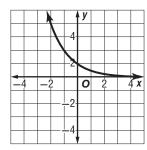
- 1. The function is continuous, one-to-one, and decreasing.
- 2. The domain is the set of all real numbers.
- **3.** The *x*-axis is the asymptote of the graph.
- **4.** The range is the set of all positive real numbers.
- **5.** The graph contains the point (0, 1).

### <u>Example</u>

# Graph $y = \left(\frac{1}{2}\right)^x$ . State the domain and range.

Make a table of values. Connect the points to form a smooth curve. The domain is all real numbers and the range is the set of all positive real numbers.

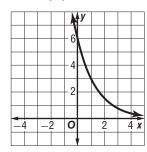
х	-2	-1	0	1	2
у	4	2	1	0.5	0.25



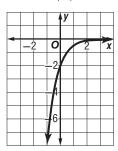
### **Exercises**

Graph each function. State the domain and range.

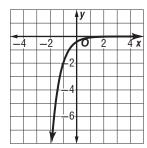
**1.** 
$$y = 6\left(\frac{1}{2}\right)^x$$



**2.** 
$$y = -2\left(\frac{1}{4}\right)^x$$



$$3. y = -0.4(0.2)^x$$



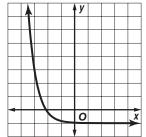
D = {all real numbers};

$$R = \{y|y > 0\}$$

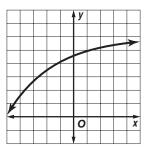
$$R = \{y | y < 0\}$$

D = {all real numbers};  
R = {
$$y|y < 0$$
}

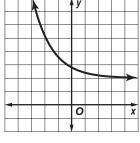
$$5. y = 4 \left(\frac{1}{5}\right)^{x+3} - 1$$



**6.** 
$$y = \left(-\frac{1}{3}\right)\left(\frac{3}{4}\right)^{x-5} + 6$$



**4.**  $y = \left(\frac{2}{5}\right)\left(\frac{1}{2}\right)^{x-1} + 2$ 



 $R = \{y | y > 2\}$ 

 $D = \{all real numbers\};$ 

 $D = \{all real numbers\};$ 

 $R = \{y | y > -1\}$ 

 $D = \{all real numbers\};$ 

 $R = \{y | y < 6\}$